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DEPT. OF POLITICAL SCIENCE UNIVERSITY OF TORONTO

630-70

MEANING, PURPOSE AND CONSTRUCTION OF INDEX NUMBERS Publications

(ca. Dec. 1937)

mise.

The following brief description of index numbers is given in response to a number of inquiries as to how the monthly indexes of retail sales as published by the Bureau may be used as a standard of comparison with individual results. The meaning of the term "Index Number" as it relates to the dollar value of retail sales may be best explained by means of a simple example.

### Retail Trade in Canada, 1930 - 1936

| Year   | Amount        | Amount as a<br>Percentage<br>of 1930<br>"Indexes" |
|--------|---------------|---|
|        | Ş             |   |
| 1930 . | 2,755,569,900 | 100.0   |
| 1931 . | 2,320,963,000 | 84.2  |
| 1932 . | 1,922,066,000 | 69.8  |
| 1933 . | 1,705,768,000 | 64.8  |
| 1934 . | 1,958,754,000 | 71.1  |
|        | 2,053,699,000 | 74.5  |
| 1936 . | 2,202,202,000 | 79.9  |

The second column in the above table shows the total dollar value of retail trade in Canada for each of the years 1930 to 1936 as obtained from the results of the annual Census of Merchandising and Service Establishments. The third column shows the sales for each of the years 1931 to 1936 expressed as percentages of the 1930 figure. These percentages which express the sales for any period in terms of those for a given constant period are known as indexes of sales. The constant period (in this case the year 1930) is known as the base period.

For some purposes the actual sales figures are of prime importance. But the trend in sales during the period under review is more readily grasped from the percentages or indexes. The indexes point out the significant movements. Hence the name - index - pointing out.

It should be noted that an index number is meaningless unless the base period is stated. Thus, while the statement that retail sales in Canada totalled \$2,202,202,000 in 1936 is significant, no meaning attaches to the fact that the index of sales for that year stood at 79.9 until it is stated that sales for 1930 formed the base upon which the comparison is made. The choice of base period may vary. Preferably the base should be a period of normal conditions. Since 1930 is the first year for which complete data on retail sales are available, sales for that year are chosen as the basis for comparisons with later periods.

Not only do the index numbers provide a ready means of comparison between any period and that chosen as the base but they also permit of comparisons between any two periods in the series. For example, sales of \$2,202,202,000 for 1936 were \$416,434,000 greater than the \$1,785,760,000 shown for 1933. The increase expressed as a percentage of the 1933 figure amounts to 23.3 per cent. The index for 1936 on the 1930 base stands at 79.9, an increase of 15.1 points or also 23.3 per cent over the index of 64.8 for 1933.

Thus for observing the general trend or for obtaining year-to-year ratios the indexes of sales may be used in exactly the same way as though the actual dollar figures were given.

#### Monthly Indexes

Indexes already explained were computed on an annual basis. They were computed by expressing the sales for each year as a percentage of sales for the one year chosen as base (in the above case, 1930). Monthly indexes are similarly computed by expressing the sales for each month as a percentage of some fixed amount. The fixed amount might be taken as the sales of any given month - say January, 1930. But January sales are low in every year as are also those for February so that indexes for all months other than the Januarys and Februarys would appear very high. Since it is only the relative change from month to month that counts, perhaps this would not matter but

it is preferable to choose a base which is independent of these wide seasonal variations. This is achieved by using as base the average monthly sales over a year or even over a period of years. The base used in the construction of the Bureau's monthly indexes of retail sales is the average monthly sales for 1930 - that is, one-twelfth the aggregate annual sales for that year. The method of construction may be described by reference to the following table in which monthly indexes are computed for the monthly sales of a fictitious departmental firm. The figures were obtained by adding together the returns of a number of moderate-sized departmental stores.

The second column contains the total dollar sales for each month from January, 1930, to October, 1937. The base figure is first obtained by totalling the twelve amounts for 1930 or \$8,456,220 and dividing the sum by 12 giving \$704,685. Each amount in Column 2 is then expressed as a percentage of \$704,685 by dividing by that figure and multiplying by 100 to clear of fractions. The resulting percentages or indexes are shown in Column 3. The indexes thus computed may be compared with the "unadjusted" indexes of department store sales shown in the monthly reports on retail sales issued by the Bureau. The comparison may best be made by charting the two series, the published averages and the individual results, on one chart. Such a comparison for the fictitious department store in the above example is shown in the attached chart, each point on the chart representing the index for a certain month as shown across the bottom. The widely fluctuating lines represent the actual monthly movements, the full lines representing the averages and the dotted lines the results for the individual firm. A comparison of the two graphs shows that not only did sales of the individual firm keep at a higher level than the average but also that its seasonal movements were much more pronounced especially in the spring months. The Bureau's indexes of departmental store sales are computed from monthly data submitted by practically all the department stores in Canada and including both store and mail order business. The inclusion of mail order sales doubtless has a considerable effect in modifying the seasonal characteristics revealed in monthly indexes of sales for department stores.

#### Corrections for Seasonal Variations

A special bulletin was issued by the Bureau two years ago explaining in considerable detail the method of constructing indexes of sales and of correcting these in order to remove seasonal variations and reveal the underlying trend. (1) A first approach to the problem can be achieved by means of moving averages which may also be explained by reference to the indexes of our fictitious departmental firm. The twelve indexes for 1930 as given in Column 3 are totalled and the total placed in Column 4 opposite the month of June, 1930. The twelve indexes starting with February, 1930, and including January, 1931, are next totalled and the result placed opposite July, 1930. In the same way totals for every twelve-month period are found and placed opposite the mid point of that period. The total for any period may be readily found from the preceding one by deducting the figure for the first month in the earlier period and adding on one new amount in the series. The first total shown in Column 4, 1200.01, is the sum of the twelve indexes for 1930. The second total, 1188.41, equals 1200.01 minus 73.19 (the index for January, 1930) and increased by 61.59 (the index for January, 1931). The third total is obtained from the second by deducting 79.05 (the index for February, 1930) and adding 63.21 (the index for February, 1931). All the figures in Column 4 may thus be found by the simple process of subtraction and addition.

Each total in Column 4 is next divided by 12 and the resulting quotients are entered in Column 5. These averages are known as twelve-month moving averages and reflect the general underlying trend with the wide seasonal swings so apparent in the original indexes completely removed. Moving averages for the individual firm and for the department store group as a whole are also shown on the attached chart.

Moving averages are deficient in that they cannot be brought up to date. From the method of their construction they are necessarily six months behind. To overcome this difficulty it is customary to compute seasonal correction factors or factors which may be applied to the unadjusted indexes in order to remove the main seasonal effects. The method used in constructing these adjustment factors is fully described in the bulletin to which reference has already been made.

(1) Monthly Indexes of Retail Sales, 1929 - 1935.

This report, explaining the method of construction of the indexes of retail sales and their adjustment for seasonal variations and containing a summary of results with illustrative charts, may be obtained from the Dominion Bureau of Statistics, Ottawa, for 50 cents.

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The second selwan converse to the total dollar sales for each mosts from January, 190, as Detober, 1937. The many liquies as lives obtained by cotalizing the country of the first for 1930 or anywhele for 1930 or anywhele as a percentage of 1904,605 by dividing by that filgures and latelying by 100 to also of fractions. The remaining percentages or indexes are anount totally in 100 to also of fractions. The remaining percentages or indexes at anount column 3. The indexes of the second of

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# Calculation of Monthly Indexes of Sales

| Col. 1   | Col. 2             | Col. 3                 | Col. 4           | Col. 5             |
|--|--------------------|------------------------|------------------|--------------------|
| Voor and March   | m                  | Indexes                | Twelve-          | Twelve-            |
| Year and Month   | Total<br>Sales     | of Sales,              | Wonth            | Month              |
|  | Dates              | Average for 1930 = 100 | Moving<br>Totals | Moving<br>Averages |
| BOTH SERVE SET SET OF THE SET SET SET SET SET SET SET SET SET SE | Ş                  | 1930 - 100             | TOPALS           | Averages           |
|  |                    |                        |                  |                    |
| 1930 - January   | 515,762            | 73.19                  |                  |                    |
| February   | 557,030            | 79.05                  |                  |                    |
| March  | 623,234            | 88.44                  |                  |                    |
| April  | 785,397<br>827,555 | 111.45                 |                  |                    |
| May  | 705,163            | 100.07                 | 1200.01          | 100.00             |
| July   | 494,131            | 70.12                  | 1188.41          | 99.03              |
| August   | 540,517            | 76.70                  | 1172.57          | 97.71              |
| September  | 771,334            | 109.46                 | 1197.44          | 99.79              |
| October  | 865,845            | 122.87                 | 1192.92          | 99.41              |
| November   | 759,970            | 107.85                 | 1193.46          | 99.46              |
| December   | 1,010,282          | 143.37                 | 1193.94          | 99.50              |
|  |                    |                        |                  |                    |
| 1931 - January   | 434,041            | 61.59                  | 1189.56          | 99.13              |
| February   | 445,454            | 63.21                  | 1181.45          | 98.45              |
| March  | 753,516            | 106.93                 | 1153.68          | 96.14              |
| May  | 831,407            | 117.98                 | 1150.16          | 95.85              |
| June   | 708,567            | 100.55                 | 1140.47          | 95.04              |
| July   | 463,255            | 65.74                  | 1135.07          | 94.59              |
| August   | 483,351            | 68.59                  | 1124.82          | 93.74              |
| September  | 675,339            | 95.84                  | 1100.34          | 91.70              |
| October  | 766,161            | 108.72                 | 1083.19          | 90.27              |
| November   | 735,219            | 104.33                 | 1066.26          | 88.86              |
| December   | 741,775            | 133,60                 | 1040+21          | 01.1               |
| 3.020 T  | 305 058            | 56.19                  | 1032.81          | 86.07              |
| 1932 - January   | 395,958<br>373,192 | 52.96                  | 1018.53          | 84.88              |
| February   | 625,982            | 88.83                  | 993.72           | 82.81              |
| April  | 632,699            | 89.78                  | 979.02           | 81.59              |
| May  | 712,113            | 101.05                 | 960.83           | 80.07              |
| June   | 568,011            | 80.60                  | 933.90           | 77.83              |
| July   | 368,126            | 52.24                  | 923.71           | 76.98              |
| August   | 382,747            | 54.31                  | 916.50           | 76.38              |
| September  | 500,517            | 71.03                  | 906.12           | 75.51              |
| October  | 662,539            | 94.02                  | 903.74           | 74.95              |
| November   | 606,984<br>752,286 | 106.75                 | 894.84           | 74.57              |
| December   | 192,200            | 100.1)                 | 0)4.01           | 1                  |
| 1022   | 221 775            | 46.00                  | 892.77           | 74.40              |
| 1933 - January<br>February                                       | 324,175            | 45.75                  | 894.42           | 74.53              |
| March  | 552,849            | 78.45                  | 908.42           | 75.70              |
| April  | 615,900            | 87.40                  | 908.39           | 75.70              |
| May  | 681,229            | 96.67                  | 906.00           | 75.50              |
| June   | 536,091            | 76.08                  | 906.78           | 75.56              |
| July   | 353,514            | 50.17                  | 914.56           | 76.21              |
| August   | 394,325            | 55.96                  | 914.39           | 76.20              |
| September  | 599,221            | 85.03                  | 926.80           | 76.92              |
| October  | 662,302            | 93.99                  | 921.70           | 76.81              |
| November   | 590,154<br>757,761 | 107.53                 | 932.37           | 77.70              |
| December   | 131,101            | 101.00                 | /55/             | 1                  |

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# Calculation of Monthly Indexes of Sales (Cont'd.) -

| Total<br>Sales | Col. 3 Indexes of Sales,   | Col. 4 Twelve- Month  | Col. 5 Twelve- Month   |
|----------------|--|---|--|
|                |  | Month   | 1  |
| Sales          |  |   | AVIET I LIST   |
|                | Average for  | Woving  | Moving   |
|                | 1930 = 100   | Totals  | Averages   |
| 9              |  | 10 00,12  | AV OI AKOS   |
|                |  |   |  |
| 378,959        | 53.78  | 937.07  | 78.09  |
|                | 45.58  | 942.11  | 78.51  |
| 640,249        | 90.86  | 935.22  | 77.93  |
| 589,177        | 83.61  |   | 77.54  |
| 671.976        |  |   | 77.48  |
|                |  |   | 78.84  |
|                |  |   | 78.78  |
|                |  |   | 78.75  |
|                |  |   | 78.12  |
|                |  |   | 79.26  |
|                |  |   | 78.91  |
|                | 1  |   | 78.93  |
| 013,030        | 143.07   | 741.4   | 10.73  |
| 272            |  |   |  |
|                |  |   | 79.31  |
|                |  |   | 79.67  |
|                |  |   | 79.74  |
|                |  |   | 80.65  |
|                |  |   | 81.10  |
|                |  |   | 81.76  |
|                |  |   | 81.02  |
|                |  |   | 81.53  |
|                | 78.95  |   | 81.53  |
|                |  |   | 81.01  |
| 623,760        | 88.52  | 975.26  | 81,27  |
| 928,741        | 131.80   | 977.23  | 81.44  |
|                |  |   |  |
| 310,455        | 44.06  | 973.98  | 81.16  |
|                |  |   | 81.21  |
| 586,783        | 83.27  | 974.12  | 81.18  |
| 640,610        | 90.91  | 976.40  | 81.37  |
| 664,893        | 94.35  | 973.44  | 81.12  |
| 627,048        | 88.98  | 975.36  | 81.28  |
| 395,864        | 56.18  | 976.18  | 81.35  |
|                | 65.83  | 974.14  | 81.18  |
|                |  |   | 81.92  |
|                |  |   | 82.32  |
|                | 1  |   | 82.68  |
|                |  |   | 83.37  |
| , -, -, -      | 331.2  |   |  |
| 316.274        | 44.88  | 1007.20   | 83.93  |
|                |  |   | 83.83  |
|                |  |   | 84.90  |
|                |  |   | 85.33  |
|                |  | 1023.70   | ٠,٠٥٥  |
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| V              |  |   |  |
| 758,337        | 107.61   |   |  |
|                | 321,185<br>640,249<br>589,177<br>671,976<br>611,295<br>386,647<br>429,832<br>550,675<br>628,587<br>585,458<br>873,038<br>373,561<br>318,840<br>536,839<br>685,320<br>642,425<br>613,165<br>418,759<br>460,381<br>556,892<br>623,760<br>928,741<br>310,455<br>362,642<br>586,783<br>640,610<br>664,893<br>627,048 | 321,185 640,249 90.86 589,177 83.61 671,976 95.36 611,295 386,647 429,832 61.00 550,675 78.14 628,587 89.20 585,458 873,038 123.89  373,561 318,840 45.25 586,839 83.28 685,320 97.25 642,425 91.16 613,165 87.01 418,759 440,381 556,361 78.95 705,892 100.17 623,760 928,741 131.80  310,455 44.06 362,642 51.46 586,783 83.27 640,610 90.91 664,893 627,048 389,98 395,864 463,914 5583,781 78.59 721,964 664,893 627,048 389,98 395,864 463,914 553,781 78.59 721,964 65.83 553,781 78.59 721,964 65,83 553,781 78.59 721,964 65,83 553,781 78.59 721,964 65,83 553,781 78.59 721,964 65,83 65,363 649,715 62,89 455,233 646,60 91.42 | 321,185       45.58       942.11         640,249       90.86       935.22         589,177       83.61       930.43         671,976       95.36       929.76         611,295       86.75       946.12         386,647       54.87       945.35         429,832       61.00       945.02         550,675       78.14       937.44         628,587       89.20       951.08         585,458       83.08       946.88         873,038       123.89       947.14              373,561       53.01       951.70         318,840       45.25       956.03         586,839       83.28       956.84         605,320       97.25       967.81         642,425       91.16       973.25         613,165       87.01       941.16         418,759       59.43       972.21         460,381       65.33       978.42         556,361       78.95       975.26         928,741       131.80       973.98         362,642       51.46       974.48         586,733       83.27       975.26         928,741       90 |

MONTHLY INDEXES OF RETAIL SALES

(Comparison of Results for an Individual Firm and Dominion Averages for Department Stores)









